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**A. P. Dioguardi¹, T. Kissikov¹, C. H. Lin¹, K. R. Shirer¹,
M. M. Lawson¹, H.-J. Grafe², J.-H. Chu^{3,4}, I. R. Fisher^{3,4},
R. M. Fernandes⁵, N. J. Curro¹, N. A. Ispulov⁶, M. K. Zhukonov⁶**

¹PhD, University of California, Davis, USA

^{1*}PhD student, University of California, Davis, USA

²PhD, IFW Dresden, Institute for Solid State Research, P.O. Box Dresden, Germany

³PhD, Stanford University, Stanford, California, USA

⁴PhD, Stanford Institute of Energy and Materials Science, California, USA

⁵PhD, University of Minnesota, Minneapolis, Minnesota, USA

⁶phys.-math.sc.candidate, S. Toraighyrov Pavlodar State University, Kazakhstan

e-mail: ⁶nurlybek_79@mail.ru

NMR EVIDENCE FOR INHOMOGENEOUS NEMATIC FLUCTUATIONS IN $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

We present evidence for nuclear spin-lattice relaxation driven by glassy nematic fluctuations in isovalent P-doped BaFe_2As_2 single crystals. Both the ^{75}As and ^{31}P sites exhibit stretched-exponential relaxation similar to the electron-doped systems. By comparing the hyperfine fields and the relaxation rates at these sites we find that the As relaxation cannot be explained solely in terms of magnetic spin fluctuations. We demonstrate that nematic fluctuations couple to the As nuclear quadrupolar moment and can explain the excess relaxation. These results suggest that glassy nematic dynamics are a universal phenomenon in the iron-based superconductors.

Keywords: inhomogeneous, nematic, fluctuation, spin-lattice relaxation, superconductors, magnetic, spectroscopy, hyperfine coupling.

INTRODUCTION

The iron-based superconductors continue to attract broad interest not only because of the presence of unconventional high-temperature superconductivity, but also because of their unusual normal state behavior [1]. As in other

unconventional superconductors the superconductivity emerges at the boundary of antiferromagnetism, suggesting an important role for antiferromagnetic fluctuations in the superconducting pairing mechanism [2, 3]. In recent years, however, significant attention has focused on the presence of nematic order that breaks the C_4 point group symmetry of the lattice at the tetragonal to orthorhombic structural transition, as well as the large nematic susceptibility in the tetragonal paramagnetic regime [4-8]. Elasto-resistance measurements indicate that the static nematic susceptibility diverges near optimal doping in several pnictide families [9, 10]. Similar conclusions are drawn from both elastic constant measurements [11] and Raman spectroscopy [12-14]. An open question, therefore, is whether there is a connection between the nematic fluctuations and the unconventional superconductivity in these materials [6, 15, 16].

MAIN PART

Experimentally the nematic fluctuations appear to be strongly coupled to the spin degrees of freedom. The shear modulus and the nuclear spin-lattice relaxation rate, T_1^{-1} , are strongly temperature and doping dependent, but scale with one another in Co- and K-doped BaFe_2As_2 [17, 18]. Assuming that the dominant channel for T_1^{-1} is via the hyperfine coupling to the Fe spins, this empirical relationship implies that the lattice and spin fluctuations have a common origin. Further evidence for a coupling between these order parameters has emerged from neutron scattering studies which reveal that C_4 symmetry is broken for the spin fluctuations in the high-temperature phase of uniaxial-strained $\text{Ba}(\text{Fe}_{1-x}\text{Ni}_x)_2\text{As}_2$ [19]. Other neutron scattering experiments have uncovered an enhancement of spin fluctuations in both LaFeAsO and $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ between the structural transition and antiferromagnetic transition temperatures [20]. In contrast, the iron chalcogenide FeSe undergoes a nematic phase transition despite the absence of long-range magnetic order down to the lowest temperatures. Although nuclear magnetic resonance (NMR) measurements do not observe significant low-energy magnetic fluctuations above the nematic transition [21, 22], neutron scattering indicates the presence of sizable spin fluctuations at moderate energies [23, 24].

Direct evidence for the nematic fluctuations has remained elusive. NMR studies of $\text{Ba}(\text{Fe}_{1-x}\text{M}_x)_2\text{As}_2$ ($M = \text{Co}, \text{Cu}$) uncovered the presence of glassy spin dynamics extending up to 100 K, with a doping and temperature response that matches that of the nematic susceptibility [25, 26]. The glassy behavior possibly originates from quenched disorder, which can act as a random local field on the fluctuating nematic order [10, 27]. In such a case, magnetoelastic coupling ensures that random variations in the local value of the nematic order parameter also affects the local spin fluctuations measured by NMR [17].

In order to investigate the presence of nematic fluctuations directly, we have investigated the NMR properties of both the ^{75}As ($^{75}\gamma = 7.2919 \text{ MHz/T}$, I

$= 3/2$, $Q = 0.31$ barns) and ^{31}P ($^{31}\gamma = 17.2356$ MHz/T, $I = 1/2$) in single crystals of $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$. Isovalent substitution of P for As in BaFe_2As_2 gives rise to superconductivity with a phase diagram that is similar to that of the electron- or hole-doped system [28, 29]. These nuclei present a unique opportunity because they are located at the same crystallographic site, but the $I = 3/2$ ^{75}As nucleus experiences a quadrupolar interaction whereas the $I = 1/2$ ^{31}P nucleus does not. Both nuclei are sensitive to magnetic hyperfine fluctuations of the Fe spins, however the As is also sensitive to fluctuations of the local electric field gradient (EFG). Nematic fluctuations couple directly to

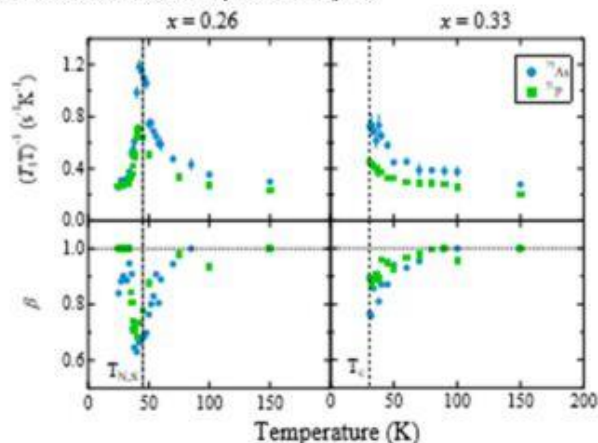


Figure 1 – $(T_1T)^{-1}$ and β for ^{75}As (•) and ^{31}P (–) vs. temperature for $x = 0.26$ (underdoped) and $x = 0.33$ (optimal doping).

EFG and give rise to an extra channel for relaxation at the As. We carefully analyze the relaxation of both nuclei, and conclude that quadrupolar fluctuations are indeed contributing to the relaxation of the As, giving rise to a maximum in the ratio $^{75}\text{T}_1^{-1} / ^{31}\text{T}_1^{-1}$ at the structural transition temperature, T_s . We also observe inhomogeneous dynamics that result in stretched exponential spin-lattice relaxation for both nuclear species. The amount of dynamical inhomogeneity is similar to previous NMR observations in both Co- and Cu-doped BaFe_2As_2 [25, 26] and LaFeAsO [30, 31] compounds.

Single crystals were synthesized via a self-flux method and characterized via transport measurements to determine P-doping levels. The P concentration x was estimated by comparison of transport properties with samples from the same and similar growth batches for which the composition had been determined via microprobe analysis [32]. The spin-lattice relaxation rates of ^{75}As and ^{31}P were measured at the central transition ($I_x = \pm 1/2$) in two $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$ crystals with

$x = 0.26$ (underdoped, $T_s = T_N = 45$ K) and $x = 0.33$ (optimally doped, $T_c = 31$ K) as a function of temperature via a standard inversion recovery pulse sequence. The crystals were aligned with the external field $H_0 = 11.7285$ T oriented perpendicular to the c-axis, and the magnetization recovery was fit to the appropriate normal modes recovery function modified by a stretching exponent β , as described in [25].

The spin-lattice relaxation rate divided by temperature $(T_1T)^{-1}$ is shown in Fig. 1 as a function of temperature for both nuclei. At high temperatures $(T_1T)^{-1}$ is roughly constant, indicating metallic Korringa behavior. In the underdoped crystal $(T_1T)^{-1}$ goes through a peak at T_N reflecting critical slowing down of the spin fluctuations. In the optimally doped crystal $(T_1T)^{-1}$ continues to increase down to T_c . These results are consistent with previously published data in polycrystalline samples [28, 29]. The relaxation rates of the two nuclei scale roughly with one another, but there are important differences that emerge at low temperature, as discussed below.

The stretching exponent, β , shown in Fig. 1, is a measure of the degree of dynamical inhomogeneity in the material [25, 26]. $\beta = 1$ indicates homogeneous relaxation whereas $\beta < 1$ indicates a distribution of local relaxation rates [33]. Both crystals and both sites become dynamically inhomogeneous below ~ 100 K, reaching down to $\beta = 0.6$ for the underdoped sample. Similar behavior was observed in other iron pnictides [30, 31]. Surprisingly, the degree of inhomogeneity does not appear to be reduced in the P-doped system as compared to the Co-doped system, despite the fact that the former is cleaner than the latter (comparisons of β in $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$ and $\text{BaFe}_2-\text{Co}_x\text{As}_2$ are available in the supplemental material).

We now turn to the relationship between the As and the P relaxation rates. Fig. 2(a) shows $^{75}\text{T}_1^{-1} / ^{31}\text{T}_1^{-1}$ as a function of temperature. This ratio is nearly constant and ~ 1.3 above approximately 60 K, indicating a common relaxation mechanism for both sites. However, below this temperature the ratio increases with decreasing temperature and reaches a maximum value of ~ 2 in both the underdoped and optimally doped crystals. The strong temperature dependence of this ratio reflects either a change in the antiferromagnetic fluctuations, or an additional relaxation mechanism present at the As site.

Spin fluctuations give rise to dynamical hyperfine fields causing nuclear spin relaxation. In order to properly extract the contribution of antiferromagnetic fluctuations to the relaxation rate, it is crucial to know the components of the hyperfine tensor, B , at both the As and the P. The hyperfine interaction is given by $H_{\text{hyp}} = \sum_{\text{Fe}} \hat{I} \cdot B \cdot S(r_i)$, where $S(r_i)$ is the electronic spin of the Fe, and \hat{I} is the nuclear spin of either the ^{31}P or ^{75}As [34]. By comparing the Knight shift and magnetic susceptibility, Kitagawa et al. found $^{75}B_{\text{aa}} = ^{75}B_{\text{bb}} = 0.66$ T/ μB , and $^{75}B_{\text{cc}} = 0.47$ T/ μB [34]. In $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$, our measurements of the Knight shift (see supplemental material) indicate that $^{31}B_{\text{aa}} / ^{75}B_{\text{aa}} = 0.40 \pm 0.02$ in agreement with a previous study [29].

It is also important to consider the off-diagonal component B_{ac} , which gives rise to the internal field at the antiferromagnetic wavevector. Previous measurements revealed that ${}^{75}B_{ac} = 0.43 \text{ T}/\mu\text{B}$ [34]. To determine this component in $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$, we measured the angular dependence of the magnetic splitting of the central line in the antiferromagnetic phase of the underdoped sample. Fig. 3 shows spectra of both the As and the P for various orientations of the crystal. The internal field, H_{int} , is oriented along $\pm\hat{c}$ -axis, giving rise to two separate resonances. The P resonances are given by: ${}^{31}f = {}^{31}\gamma(1 + K)(H_0 \pm H_{\text{int}} \cos \theta)$, where K is the Knight shift and θ is the angle between \hat{c} and H_0 . For the As, there is an additional shift due to the quadrupolar interaction: ${}^{75}f = {}^{75}\gamma(1 + K)(H_0 \pm H_{\text{int}} \cos \theta) + \Delta_Q(1 - 9 \cos^2 \theta)(1 - \cos^2 \theta)$, where $\Delta_Q = \frac{2}{3}e^2Q^2V_{zz}^2/{}^{75}H_0$, Q is the quadrupolar moment and V_{zz} is the component of the EFG tensor at the As [35]. Fitting the angular dependent spectra, we extract internal fields ${}^{75}H_{\text{int}} = 0.45 \pm 0.01 \text{ T}$ and ${}^{31}H_{\text{int}} = 0.100 \pm 0.001 \text{ T}$, yielding ${}^{31}B_{ac}/{}^{75}B_{ac} = 0.226 \pm 0.007$. It is noteworthy that the transferred hyperfine couplings to the P are less than those to the As, which probably reflect the fact that the 4p orbitals at the As are more extended. Previous studies of the hyperfine couplings at the As and P sites in other compounds have found a similar ratio [36].

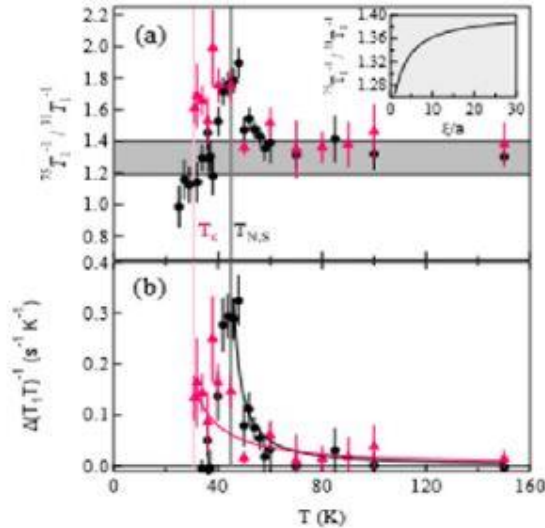


Figure 2 – (a) Ratio of the spin lattice relaxation rates of As to P (${}^{75}T_1^{-1}/{}^{31}T_1^{-1}$) and (b) $\Delta(T_1T)^{-1}$ vs. temperature for $x = 0.26$ (●) and $x = 0.33$ (▲). The gray horizontal region indicates the range of values for purely magnetic fluctuations. INSET: The theoretical ratio as a function of the antiferromagnetic correlation length, ξ . Solid lines in (b) are best fits as discussed in the text.

With the knowledge of the hyperfine couplings, it is now possible to compute the magnetic component of the spin-lattice relaxation rate:

$$W_0 = \gamma^2 k_B T \lim_{\omega \rightarrow 0} \sum_{q, \alpha, \beta} F_{\alpha\beta}(q) \frac{\text{Im} \chi_m^{\alpha\beta}(q, \omega)}{\hbar \omega}, \quad (1)$$

where $F_{\alpha\beta}(q)$ are the form factors (given in the Supplemental Material), $\chi_m^{\alpha\beta}(q, \omega)$ is the dynamical magnetic susceptibility, and $\alpha, \beta = \{a, b, c\}$ [37]. For purely magnetic fluctuations, $T_1^{-1} = 2W_0$. Because the hyperfine coupling ratios ${}^{31}B_{aa}/{}^{75}B_{aa}$ and ${}^{31}B_{ac}/{}^{75}B_{ac}$ are not the same, the form factors $F_{\alpha\beta}(q)$ for the two sites do not simply scale with one another. As a result, the ratio ${}^{75}T_1^{-1}/{}^{31}T_1^{-1}$ will depend of the detailed q -dependence of $\chi_m^{\alpha\beta}(q, \omega)$, which can change with temperature. To estimate the effect of antiferromagnetic correlations on the T_1^{-1} ratio, we use Eq. 1 and the dynamical magnetic susceptibility:

$$\chi_m^{\alpha\alpha}(q, \omega) = \sum_{j=1,2} \frac{\chi_{\alpha\alpha}(Q_j)}{1 + |q - Q_j|^2 \xi^2 - i\omega/i\omega_{sf}}, \quad (2)$$

where ξ is the antiferromagnetic correlation length, ω_{sf} is the characteristic spin fluctuation frequency, and $\chi_{\alpha\alpha}(Q_j)$ is the value of the susceptibility at the ordering wavevectors $Q_1 = \{\pi/a, 0\}$ and $Q_2 = \{0, \pi/a\}$ [19, 38]. The inset of Fig. 2 (a) shows the calculated T_1^{-1} ratio as a function of correlation length, with the following assumptions: (i) ${}^{31}B_{cc}/{}^{75}B_{cc} = {}^{31}B_{aa}/{}^{75}B_{aa}$, (ii) B_{ab} is negligible, and (iii) $\chi_{\alpha\alpha}(Q_j)$ is the same for all values of i and α (isotropic fluctuations). This quantity changes only slightly with ξ , varying between 1.19 ($\xi = 0$) to 1.40 ($\xi = \infty$), as shown by the gray area in Fig. 2 (a). For the underdoped sample, the experimental ratio exceeds this prediction below the structural transition, reaching up to ~ 2 at T_N . The experimental ratio for the optimally doped sample reaches the same value just above T_c . It is clear that magnetic fluctuations alone cannot explain this large increase, suggesting that there is an additional relaxation channel affecting the As site.

Since the ${}^{75}\text{As}$ has spin $I = 3/2$ it is susceptible to relaxation by fluctuations of the EFG through the quadrupolar coupling. Quadrupolar spin-lattice relaxation of nuclear spins with $I > \frac{1}{2}$ is described by the Hamiltonian:

$$H_Q(t) = \frac{eQ}{4I(2I-1)} \sum_{k=-2}^2 V_k(t) \hat{T}_{2k}, \quad (3)$$

where \hat{T}_{2k} are the spherical tensor operators, $V_0 = V_{zz}$, $V_{\pm 1} = V_{zx} \pm iV_{zy}$, $V_{\pm 2} = \frac{1}{2}(V_{xx} - V_{yy}) \pm iV_{xy}$, and $V_{\alpha\beta}$ are the components of the EFG tensor [35]. The simultaneous presence of both magnetic and quadrupolar fluctuations has been discussed in detail by Suter, who has shown that these fluctuations give rise to three relaxation channels for the nuclear spins, one purely magnetic and two

quadrupolar [39]. The magnetic relaxation channel is described by Eq. 1, and the

quadrupolar relaxation rates are given by: $W_{1,2} = \left(\frac{eQ}{\hbar}\right)^2 \int_{-\infty}^{\infty} \langle V_{+1,2}(\tau) V_{-1,2}(0) \rangle e^{i\omega\tau} d\tau$.

There are two components to the EFG at the As, one from the lattice orthorhombic distortion and the other from unequal populations of the As $4p_{x,y}$ orbitals, such that $V_{-1} = 0$ and $V_{\pm 2} = V_{\pm 2}^{lat} + V_{\pm 2}^{4p}$ [40]. From the definition, we see that $(V_{+2} + V_{-2})$ has B_{2g} symmetry, whereas $i(V_{+2} - V_{-2})$ has B_{1g} symmetry (in the coordinate system of the crystallographic tetragonal unit cell). Thus, the former couples directly to the nematic order parameter. Using the fluctuation-dissipation theorem, we can express the quadrupolar relaxation rate in terms of the dynamical nematic susceptibility χ_n :

$$W_2 = \left(\frac{eQ}{\hbar}\right)^2 k_B T \lim_{\omega \rightarrow 0} \sum_q \frac{\text{Im} \chi_n(q, \omega)}{\hbar \omega} \quad (4)$$

Note that χ_n is defined in terms of the EFG, and that there is no form factor for the nematic fluctuations because the on-site orbital occupations are the dominant contribution to the EFG. The nematic fluctuations order at $q = (0, 0)$ with Curie-Weiss behavior, and the existence of a Fermi surface implies Landau damping [5, 9]. We estimate the magnitude of W_2 by considering the static EFG at the As site. In the orthorhombic phase, $V_{\pm 2}$ develops a finite value reflecting the static nematic order [34]. If we assume that the lattice, orbital and spin degrees of freedom have a similar power spectrum, then ratio of the quadrupolar to magnetic relaxation rates is $W_2/W_0 \sim (eQ\bar{V}_2 / \hbar\bar{h})^2$, where \bar{V}_2 and \bar{h} are the root mean square of the EFG and hyperfine field fluctuations, respectively. Previous field-dependent studies in $\text{BaFe}_{2-x}\text{Co}_x\text{As}_2$ found $\bar{h} \sim 40$ G [26]. $eQ\bar{V}_2 / \hbar$ reaches a static value of 2.6 MHz in the orthorhombic phase of the parent compound [34], and a value of ~ 0.3 MHz at the structural transition in $\text{BaFe}_2(\text{As}_{0.96}\text{P}_{0.04})_2$ [40]. We estimate W_2/W_0 can reach a maximum of ~ 8.4 at $T_s = T_N$, thus it is clear that both magnetic and nematic fluctuations are of comparable magnitude and can contribute to the spin-lattice relaxation of the As. We conclude that the enhanced temperature dependent ratio seen in Fig. 2(a) reflects the presence of nematic fluctuations.

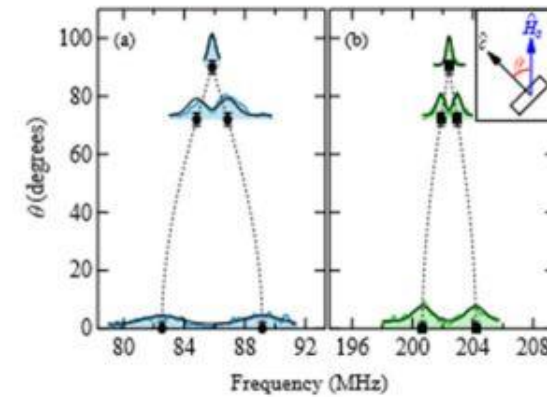


Figure 3 – Spectra of the central resonance of the ^{75}As (a) and ^{31}P (b) as a function of angle θ with respect to the c -axis for $x = 0.26$. Markers represent the centers of the respective peaks extracted from global fits (solid black lines) to each of three data sets at 0° , 72° and 90° . Dashed black lines show the calculated angular dependence of the resonance centers of the peaks based on extracted fit coefficients for the internal fields.

Note that in the presence of both quadrupolar and magnetic fluctuations, the two relaxation rates W_0 and W_2 become entangled and the exact form of the magnetization recovery becomes complex [39]. Attempts to fit the recovery data to a modified relaxation form with W_2 as a floating parameter do not necessarily lead to a better quality of fit as measured by the χ_2 value. Such fits have poor precision because both relaxation rates W_0 and W_2 follow a broad distribution function, thus the relaxation curve is stretched. This distribution is evident in the P relaxation, which has no quadrupolar relaxation channel but still exhibits stretched recovery. Thus the difference $\Delta(T_1 T)^{-1} = {}^{75}(T_1 T)^{-1} - k({}^{31}T_1 T)^{-1}$, where $k = 1.31$ is the high temperature ratio of the As to P relaxation rates is not simply proportional to W_2 . Yet, in order to assess qualitatively the contribution from W_2 , we can still focus on this quantity, plotted in Fig. 2 (b), since $W_2 = 0$ would imply $\Delta(T_1 T)^{-1} = 0$.

It is clear from Fig. 2 (b) that nematic fluctuations are present in both the underdoped and optimally-doped samples. In the underdoped crystal, the tetragonal-orthorhombic phase transition T_s coincides with T_N , and the nematic fluctuations diverge at this phase transition [41]. The solid lines through the data points are best fits to the expression $\Delta(T_1 T)^{-1} = A/(T - T_0)^n$, where for the underdoped crystal $n = 1.4 \pm 1.1$ and $T_0 = 41.5 \pm 5.7$ K. In the optimally doped sample, the data reveal that nematic fluctuations are present in the tetragonal phase down to T_c . The best fit through the data points yields $n = 1.5 \pm 1.9$ and $T_0 = 13 \pm 33$ K. Although the exact relationship between $\Delta(T_1 T)^{-1}$ and $W_2 \propto \chi_n$ is not known, it is

interesting to note that this result is consistent with elastoresistance measurements, which indicate an enhanced χ_n near a putative quantum critical point [10].

An alternative explanation for the behavior of the T_1^{-1} ratio in Fig. 2(a) is that the spin fluctuations are locally suppressed at the P sites. In this case, the As relaxation would not be enhanced by nematic fluctuations, but rather the P relaxation rate would be suppressed. A recent comparison of NMR of ^{63}Cu and ^{75}As in $\text{Ba}(\text{Fe}_{1-x}\text{Cu}_x)_2\text{As}_2$ revealed a slightly reduced relaxation at the Cu site [42]. However, the form factor and hyperfine couplings to the Cu are different than the As, which could explain the difference. Furthermore, since $^{63}\text{Q} < ^{75}\text{Q}$, it is possible that this difference reflects the reduced quadrupolar interaction at the Cu sites. Thus, our results indicate that $^{75}(\text{T}_1\text{T})^{-1}$ always contains a contribution from nematic fluctuations. The extent to which these fluctuations affect the expected Curie-Weiss behavior $^{75}(\text{T}_1\text{T})^{-1} \propto (\text{T} - \text{T}_\text{N})^{-1}$ near a magnetic transition remains to be further investigated. For instance, in systems with split nematic and magnetic transitions, such as NaFeAs and $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$, $^{75}(\text{T}_1\text{T})^{-1}$ seems to display no additional peaks at T_s , suggesting that W_2 may be subleading compared to W_0 , at least in those materials.

The approach we have taken using the susceptibility in Eq. 2 to estimate the magnetic contribution to the relaxation is essentially identical to a recent study using selfconsistent renormalization spin-fluctuation theory (SCR) [29]. In the previous study, the authors found that the spin fluctuations evolve with doping and exhibit quantum critical behavior near optimal doping for superconductivity. These antiferromagnetic spin fluctuations may provide the pairing glue for the superconductivity [3]. Our results indicate that these spin fluctuations are accompanied by nematic fluctuations in the optimally doped sample. It is possible that the nematic fluctuations may also be important for the superconducting mechanism [15].

It is interesting to consider why the inhomogeneous glassy behavior is unaffected by isovalent P doping on the As site rather than electron doping at the Fe site. Elastoresistance measurements of the nematic susceptibility find Curie-Weiss behavior over a broad range of temperatures in various doped iron pnictides [10]. However, at low temperatures in both the electron and hole doped systems, the nematic susceptibility exhibits a deviation from Curie-Weiss behavior that may arise from quenched disorder. The P-doped system, on the other hand, showed no such deviation suggesting that this system contains the least amount of disorder. Our NMR results show no distinction and indicate a similar glassy distribution of relaxation rates in P, Co and Cu doped systems. It is likely that doping at the As site still disrupts the exchange interaction between the Fe orbitals, providing a source of frustration. Alternatively, these results could also indicate that the

electronic glassiness is driven by frustrated interactions rather than chemical inhomogeneity [43].

CONCLUSION

To summarize, we have measured the hyperfine couplings and spin lattice relaxation rates of the As and P sites in $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$. We find that spin fluctuations alone are insufficient to explain the ratio between the relaxation rates at these two sites, however critical slowing down of nematic fluctuations in the tetragonal phase that couple to the quadrupolar moment of the As can explain the enhanced relaxation at the As site. In contrast to torque magnetometry and optical measurements, our results show no evidence for a phase transition above T_s , however the critical fluctuations persist well above the structural transition [44, 45]. Furthermore, the presence of inhomogeneous strain distributions in the tetragonal phase may be responsible for the distribution of relaxation rates that we observe.

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А. П. Дайгарди¹, Т. Кисиков¹, Ц. Х. Лин¹, К. Р. Ширер¹, М. М. Лоусон¹, Х.-Дж. Грэйф², Дж.-Х. Чу^{3,4}, И. Р. Фишер^{3,4}, Р. М. Фернандес⁵, Н. Дж. Куро¹, Н. А. Испулов⁶, М. К. Жукенов⁶

$BaFe_2(As_{1-x}P_x)_2$ бір текті емес нематикалық флуктуациялардың ЯМР дәлелі

¹Калифорния университеті, Дэвис, АҚШ;

²Қатты дене физикасының институты, Дрезден, Германия;

³Стэнфорд университеті, Стэнфорд, Калифорния, АҚШ;

⁴Энергия және материалтану Стэнфорд институты, Калифорния, АҚШ;

⁵Миннесота университеті, Миннеаполис, Миннесота, АҚШ;

⁶С. Торайғыров атындағы

Павлодар мемлекеттік университеті, Павлодар, Қазақстан.

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А. П. Дайгарди¹, Т. Кисиков¹, Ц. Х. Лин¹, К. Р. Ширер¹, М. М. Лоусон¹, Х.-Дж. Грэйф², Дж.-Х. Чу^{3,4}, И. Р. Фишер^{3,4}, Р. М. Фернандес⁵, Н. Дж. Куро¹, Н. А. Испулов⁶, М. К. Жукенов⁶

ЯМР доказательства неоднородных нематических флуктуаций в $BaFe_2(As_{1-x}P_x)_2$

¹Калифорнийский университет, Дэвис, США;

²Институт физики твердого тела, Дрезден, Германия;

³Стэнфордский университет, Стэнфорд, Калифорния, США;

⁴Стэнфордский институт энергии и материаловедения, Калифорния, США;

⁵Университет Миннесоты, Миннеаполис, Миннесота, США;

⁶Павлодарский государственный университет имени С. Торайғырова, Павлодар, Казахстан.

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Біз нематикалық изовалентті Р-легирленген $BaFe_2As_2$ монокристалдарда, шыны тәрізді тербелістермен шартталған, ядролық спин-торлық релаксацияның дәлелін ұсынамыз. Екі объекті де ^{75}As және ^{31}P электронды-легирленген жүйелерге ұқсас созылған экспоненциалды релаксацияға ие. Осы жерлердегі аса жұқа өрістер мен релаксация жылдамдықтарын салыстыра отырып, біз As релаксациясы біріңғай магниттік спиндік флуктуация терминдерінде түсіндіріле алмайтынын аңғарамыз.

Біз нематикалық тербелістердің ядролық квадрупольдік момент сияқты бірігетінін және артық релаксацияны түсіндіре алатындығын демонстрациялаймыз. Бұл нәтижелер шыны тәрізді қозғаушы күштердің темір негізіндегі асқын өткізгіштерде болатын әмбебап құбылыс екендігін көрсетеді.

Мы представляем доказательства ядерной спин-решеточной релаксации, обусловленной стеклообразными колебаниями в нематических изовалентных Р-легированных $BaFe_2As_2$ монокристаллах. Оба объекта ^{75}As и ^{31}P обладают растянутой экспоненциальной релаксацией, похожей на электронно-легированные системы. Сравнивая сверхтонкие поля и скорости релаксации в этих местах мы находим, что релаксация As не может быть объяснена исключительно в терминах магнитных спиновых флуктуаций. Мы демонстрируем, что нематические колебания соединяются как ядерный квадрупольный момент и могут объяснить избыточную релаксацию. Эти результаты свидетельствуют о том, что стекловидные нематические движущие силы – это универсальное явление в сверхпроводниках на основе железа.